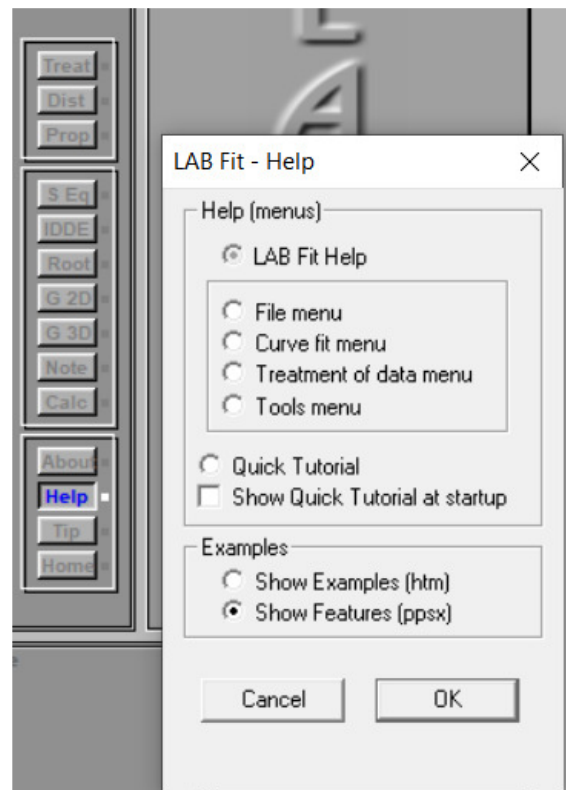
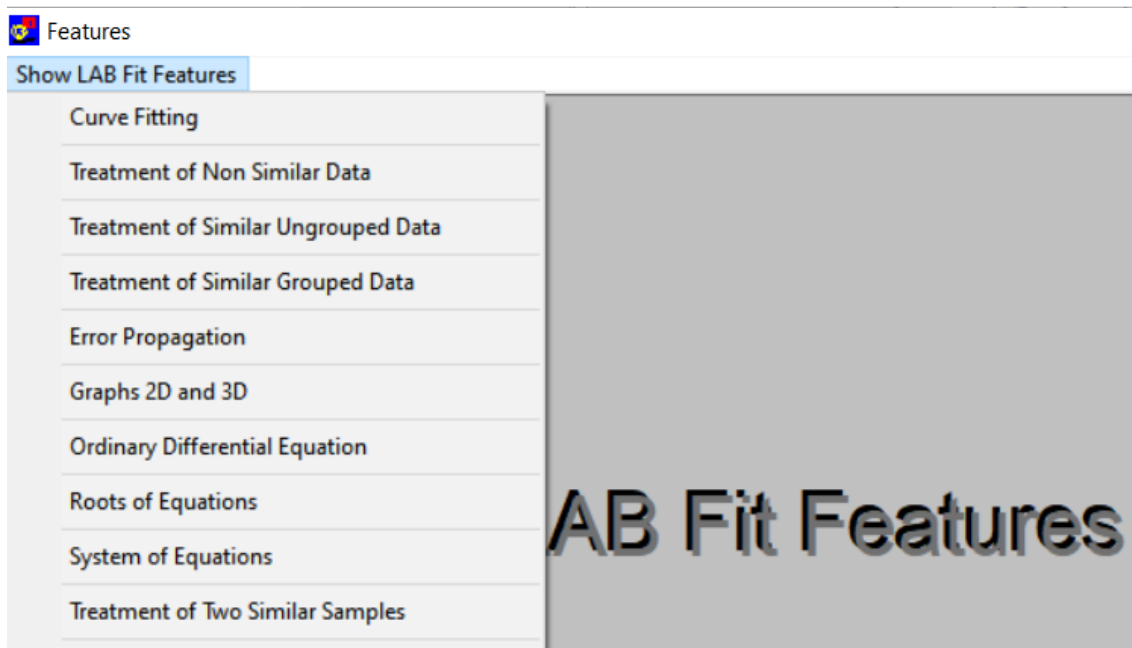


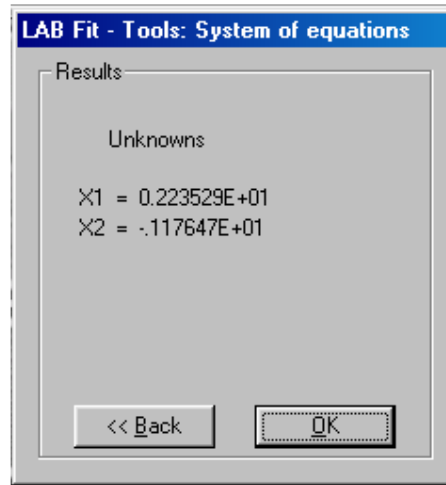
Clicking "Help" and choosing "Show Features (ppsx)"...



...you will watch several movies with help about...



After informing the coefficients of the system of equations, click on “OK” that the results will be shown at a dialog box:

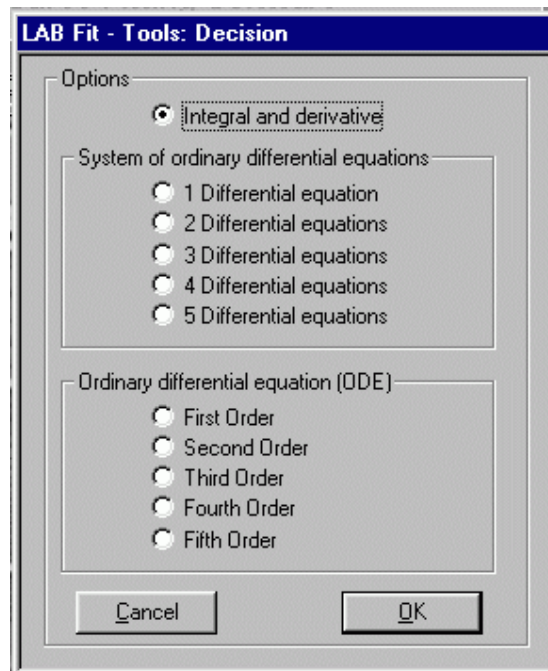


If there is need to access the informed data set, click on the “Back” button.

Integral, derivative and ODE (IDDE)

Integral and derivative

To determine the numerical value of the defined integral of a function and also its first and second derivatives for a value of X, the user must, at the “Tools” menu, click on “Integral, derivative and ODE” or also on the “IDDE” button. Then, the following dialog box will appear:



Choosing the "Integral and derivative" option and clicking on the "OK" button the following dialog box will appear:

The dialog box is titled "LAB Fit - Tools: Integral and Derivative". It contains the following fields and buttons:

- Information:** A large text input field for the function $Y =$ (independent variable: X). Below it, a note says "(up to 94 characters)". To the right, it lists "Operations: +, -, *, /, ** (power)".
- Integral:** Two input fields for "lower: $X =$ " and "upper: $X =$ ".
- Derivative:** An input field for $X =$ with a note "(first and second order)".
- Buttons:** "Cancel", "Graph", "Syntax", and "OK".

At the first edit box **the function** that is under study must be written, **in Fortran**. At the second and third boxes the integration **limits** must be written and, at the last one, the **value of X** of the derivatives that will be determined. After, click on "OK".

Ordinary Differential Equation (ODE)

To determine the numerical solution of an ordinary differential equation up to the fifth order (or a system, up to five first order equations) you must supply the necessary information on the dialog box and click on the "OK" button.

The dialog box is titled "LAB Fit - Tools: Differential Equation". It contains the following fields and buttons:

- Differential Equation:** A text box showing the general form: $y^{(5)} + f(x,y) y^{(4)} + g(x,y) y^{(3)} + r(x,y) y'' + s(x,y) y' = t(x,y)$.
- Settings:**
 - Input fields for $x_0 =$ and $x_f =$.
 - Input field for "Number of subdivisions of the interval: $N =$ " with a note "(A great value for N implies in slowness)".
 - Input fields for $t(x,y) =$, $y(x_0) =$, $f(x,y) =$, $y'(x_0) =$, $g(x,y) =$, $y''(x_0) =$, $r(x,y) =$, $y'''(x_0) =$, and $s(x,y) =$, $y^{(4)}(x_0) =$.
 - A note: "(Each function: up to 150 characters)".
- Buttons:** "Cancel", "Syntax", and "OK".

Then a new dialog box will appear and you can access the **file** with the (x,y) points referring to the **numeric solution (Runge-Kutta, fourth order)**.

Attention: If your ODE is **not adequate** for the general form shown on the dialog box, you must transform it into a **first order system**.

Approximate solution for an ODE

You can try to determine an approximate function, with up to four parameters, for the numeric solution of an ordinary differential equation (ODE) by using **curve fitting**. For this purpose, execute the following steps:

- 1) Select and copy the points from the file with the numeric solution. If it is possible, eliminate points with abscissa (or ordinate) smaller or equal to zero;
- 2) Close the ODE option ("Close" button) ;
- 3) Click on the "New" button to fit the data;
- 4) Use the "Paste" option to inform the data;
- 5) Click on the "Find" button to select the functions;
- 6) Click on the "Libr" button to fit the selected function;
- 7) If X_0 has a value between X_{min} and X_{max} you must solve the problem twice, appending together the following results: a) from X_0 up to $X_f = X_{min}$ b) from X_0 up to $X_f = X_{max}$.

An Example

$y'' + 0.5y' = \sin(y)$, with $y(0.0)=0.0$, $y'(0.0)=-1.0$, from $X_0=0.0$ up to $X_f=1.0$

Clicking on the "IDDE" button and choose the "Second Order" option (from Ordinary Differential Equation (ODE)) the following dialog box will appear:

LAB Fit - Tools: Differential Equation

Differential Equation: Second Order
 $y'' + f(x,y) y' = t(x,y)$

Settings

xo = 0 xf = 1 Number of subdivisions of the interval: N = 1500
(A great value for N implies in slowness)

t(x,y) = sin(y) y(xo) = 0.0

f(x,y) = 0.5 y'(xo) = -1.0

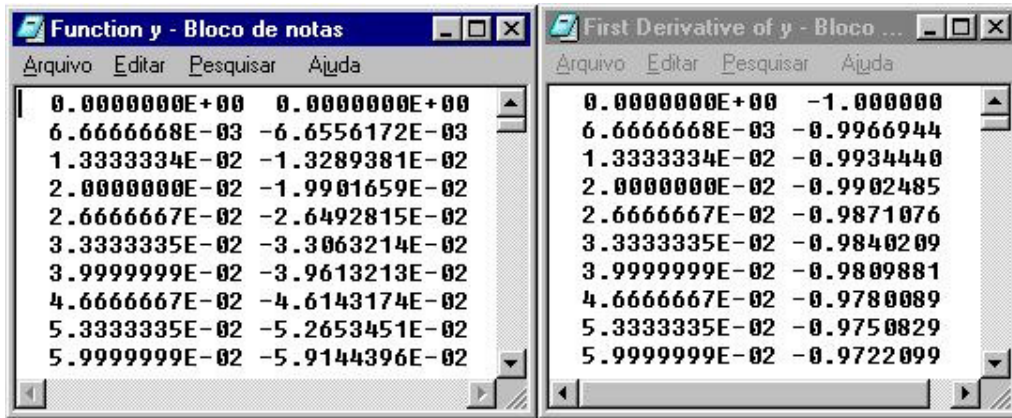
[Each function: up to 150 characters]

Cancel Syntax OK

so you can supply the necessary information about the ODE. Then, two files are obtained:

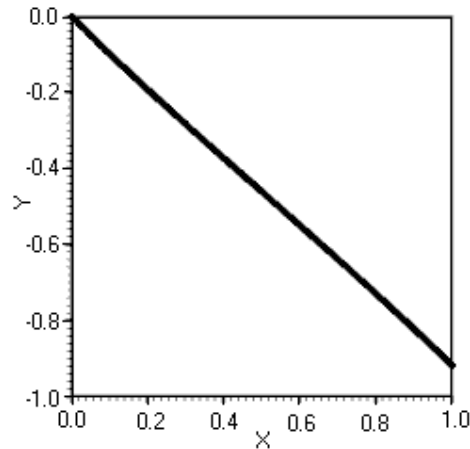
- 1) One with the points of $y(x)$;
- 2) Another with points of the first derivative $y'(x)$.

See a part of the (x,y(x)) file and of the (x,y'(x)) file:



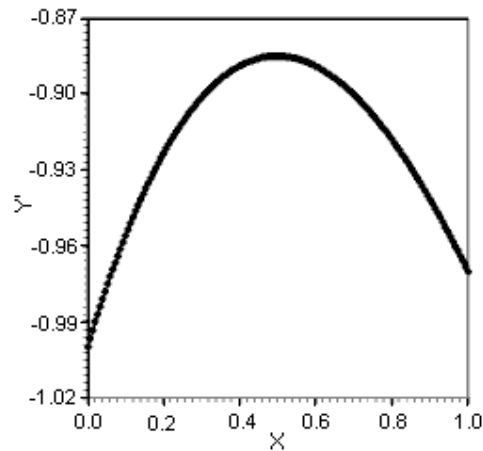
Accomplishing the seven steps indicated previously for each obtained file, at the end, the following **approximate function** is determined with four parameters (in the step 6 you should set **POWER = 50**):

$$y_{\text{appr}} = 0.5133e^{-1.2037x} - 0.5135e^{0.7366x}$$



With the same seven steps **an approximate function** is determined for the first derivative:

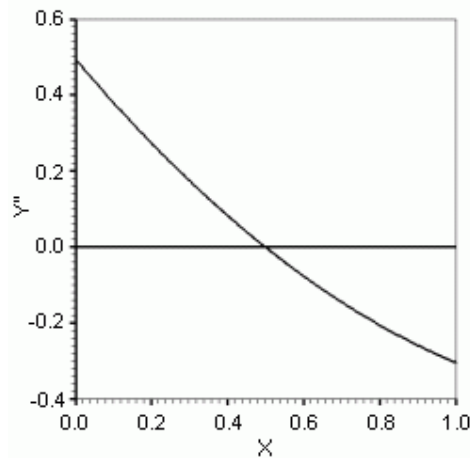
$$y'_{\text{appr}} = -0.999703 + 0.49339x - 0.5918x^2 + 0.12798x^3$$



In this example, the results were so good that it is not possible to differentiate the line that represents the **approximate function** (and its **first derivative**) from the points referring to the numeric solution.

Attention: The Runge-Kutta method does not determine values referring to the second derivative of the function obtained from a second order ODE but, if you want it, you could obtain that by direct derivation of the approached function for the first derivative, $y'_{\text{appr}}(x)$:

$$y''_{\text{appr}} = 0.49339 - 1.1836x + 0.38394x^2$$



For verification purposes of the obtained results, you could determine y , y' and y'' for $x=0$, $x=0.5$ and $x=1.0$ (from the approximate functions) which gives the following result:

$y_{\text{appr}}(0.0)=-0.0002$	$y'_{\text{appr}}(0.0)=-0.9997$	$y''_{\text{appr}}(0.0)=0.4934$
$y_{\text{appr}}(0.5)=-0.4610$	$y'_{\text{appr}}(0.5)=-0.8850$	$y''_{\text{appr}}(0.5)=-0.0024$
$y_{\text{appr}}(1.0)=-0.9186$	$y'_{\text{appr}}(1.0)=-0.9701$	$y''_{\text{appr}}(1.0)=-0.3063$

You can observe that, for these results, with small tolerance, the ordinary differential equation of this example **is verified**.

Fortran Syntax

Operations:

Addition: +

Subtraction: -

Multiplying: *

Division: /

Power: ** or ^

Functions applied to a value x

Sine of x: **sin(x)**

Cosine of x: **cos(x)**

Tangent of x: **tan(x)**

Arc which the sine is x: **asin(x)**

Arc which the cosine is x: **acos(x)**

Arc which the tangent is x: **atan(x)**

Hyperbolic Sine of x: **sinh(x)**

Hyperbolic Cosine of x: **cosh(x)**

Hyperbolic Tangent of x: **tanh(x)**

Sine of x (x in degrees): **sind(x)**

Cosine of x (x in degrees): **cosd(x)**

Tangent of x (x in degrees): **tand(x)**

Natural Logarithm of x: **log(x)**

Logarithm of x at the base 10: **log10(x)**

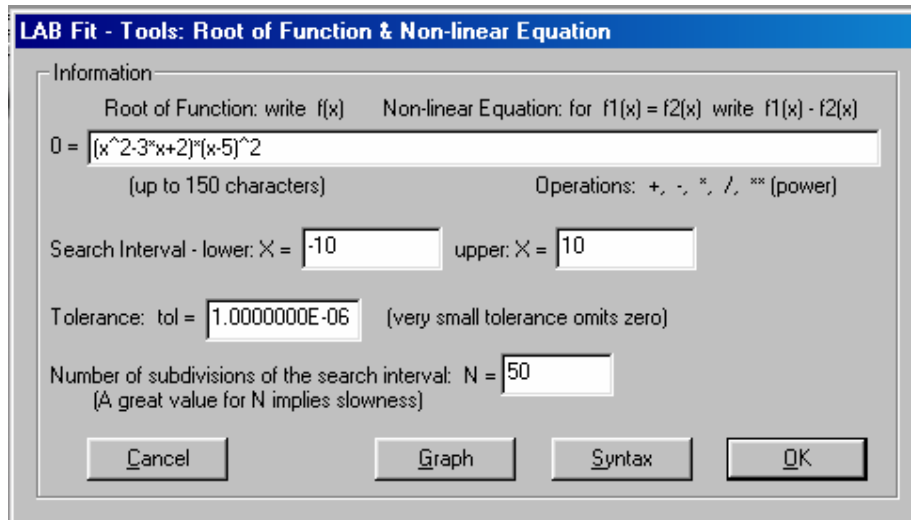
Exponential of x (e powers x): **exp(x)**

Root square of x: **sqrt(x)**

Absolute value of x: **abs(x)**

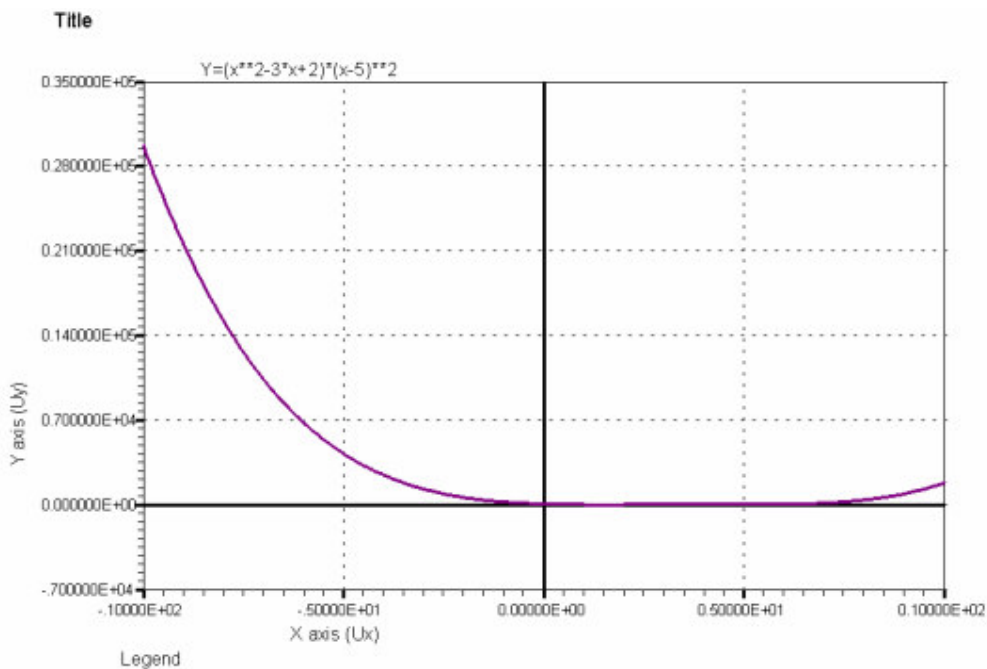
Roots of functions (Root)

To determine the roots of a function the user must, at the "Tools" menu, click on the "Zeroes of functions" option , or at the "Root" option. Then, the following dialog box will appear:

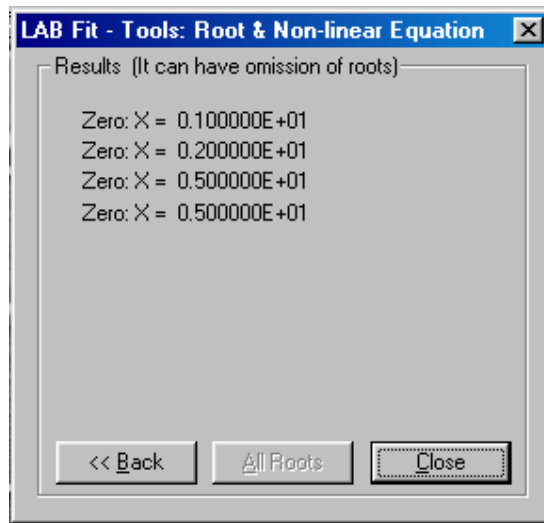


At the **first** edit box the **function** must be written. At the **two following dialog boxes**, the user must indicate the **interval limits** in which the roots search will be performed. At the **fourth** edit box, the user must write the tolerance (the default value is 1.0E-06) and, **at the last one, the number of subdivisions** of the interval, into which ones, the bisection method will be applied (the default is N = 10 but it was changed to N=50).

In case the user does not have a clear idea if the pointed interval is suitable or not, the “Graph” button can be clicked and it will be possible to see the function plotted for the given interval. For the information of the previous dialog box, we have:

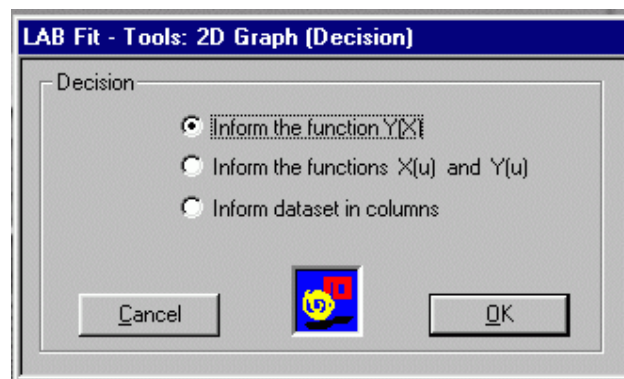


It becomes clear, then, that if there are any roots, they must be at the interval between $X = -1,0$ and $7,5$ (because this is the region where the graph touches or crosses the X axis). Then, when we close the window with the graph, it will be automatically returned to the dialog box shown previously, the interval limits must be rewritten with the new values. When “OK” is clicked, the results will be shown:



2D Graph: User model (G 2D)

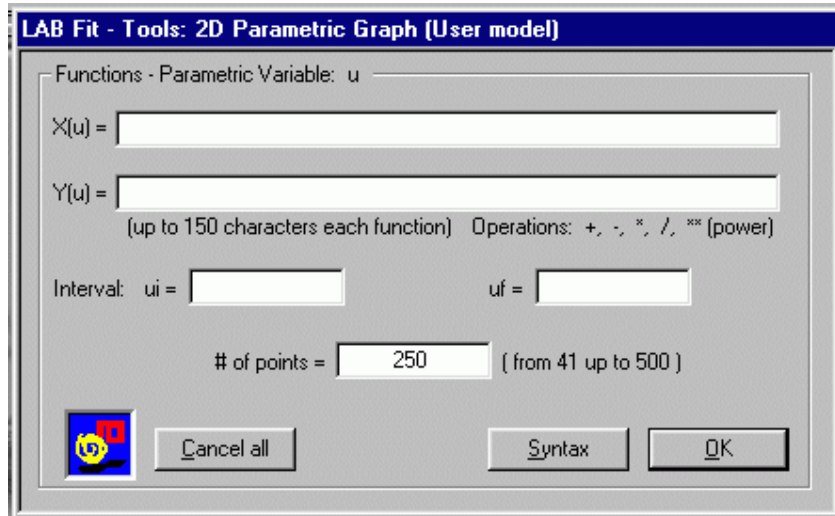
To plot the graph of a function with 1 independent variable, the user must, at the “Tools” menu, click on the “2D Graph: User model” option, or then at the “G 2D” button. Then, the following dialog box will appear:



The user has, then, the option of **informing the function** (normal or parametric) or **importing a point set to be linked**.

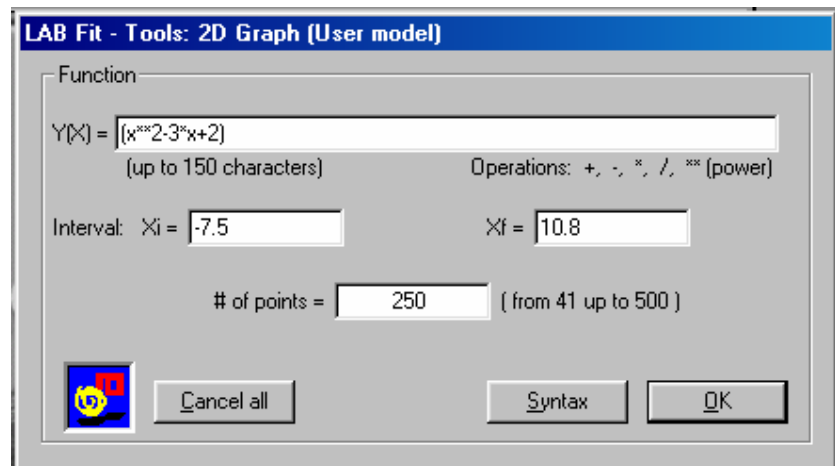
The second case, when “OK” is clicked, the dialog box for the files’ selection will appear (browse), and the user must indicate the **non-formatted** file with the points in columns.

At the first case, when “OK” is clicked for the **parametric function**, the following dialog box will appear:

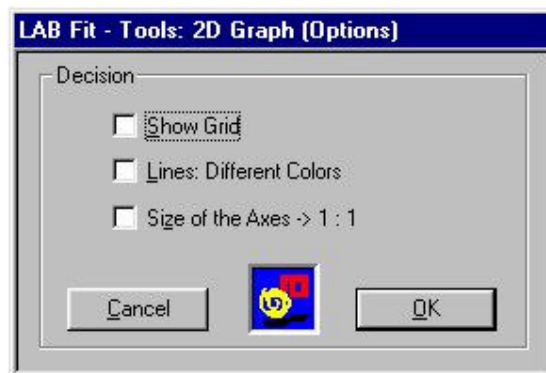


Then you must to inform $X(u)$, $Y(u)$ and the limits for the variable u .

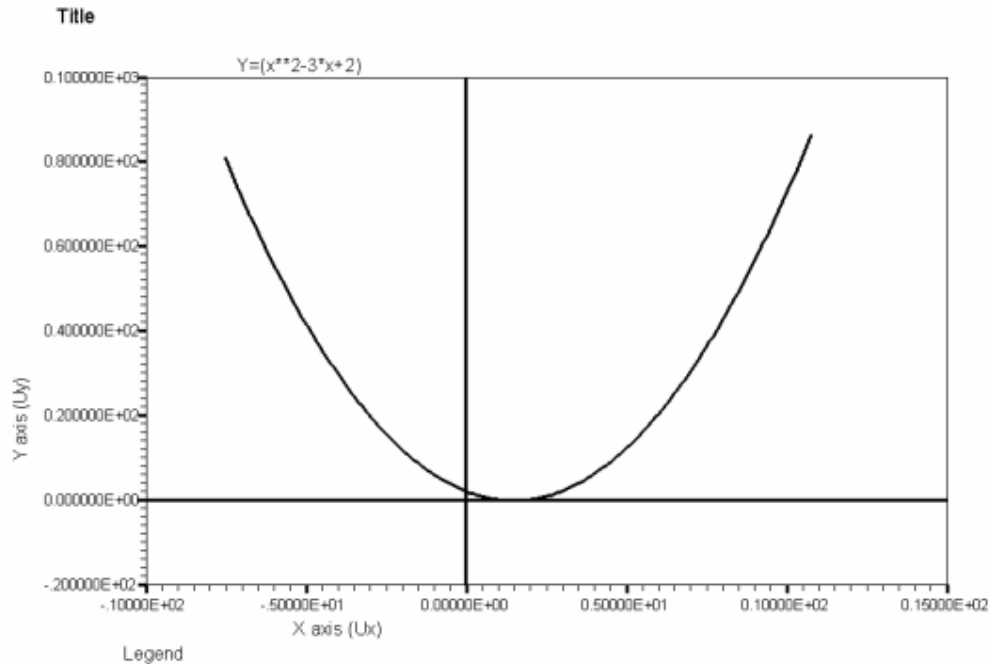
At the first case, when “OK” is clicked for the **function normally written**, the following dialog box will appear:



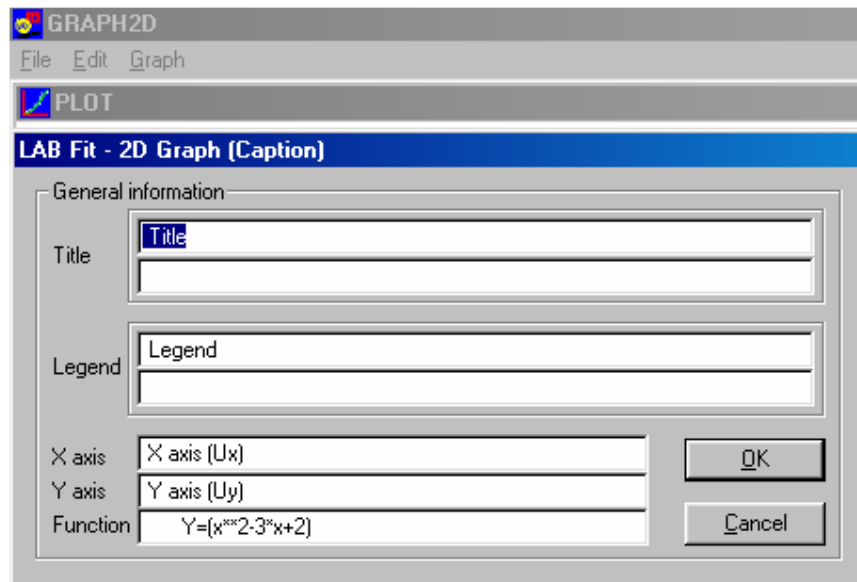
When “OK” is clicked, the question if it is desired to draw another graph will appear (it can be possible to plot up to 3 graphs simultaneously). Answering no, a new box for the definition of how the graph must be plotted will appear:



When “OK” is clicked, the plotted graph will appear:



At the same time that the 2D graph is being plotted, a dialog box appears with the graph final characterization (title, legend, axis and function definition):

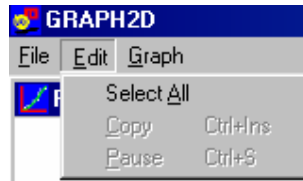


Once the 2D graph is characterized, there are two options to print it.

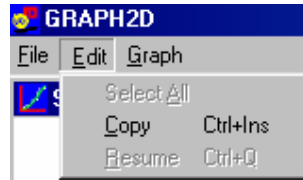
To use the **first option**, click on "Print window", at the "File" menu, but this option is used to print only a **sketch**, because the printing will not have a good quality: the printed picture will have the same resolution shown on screen.

The **second option** makes possible to print a graph **with a better quality than the previous one**, what can be done by clicking on the "Superzoom in" item at the "Graph" menu. The graph will be, then, plotted again, but with a much higher resolution than the original one, using a much bigger space than the available screen size. After that, at the "File" menu, the user must click on "Print graph (superzoom)".

To **paste** the graph, the user must choose, at the “**Edit**” menu, the “**Select All**” option as it is shown at the picture at next:



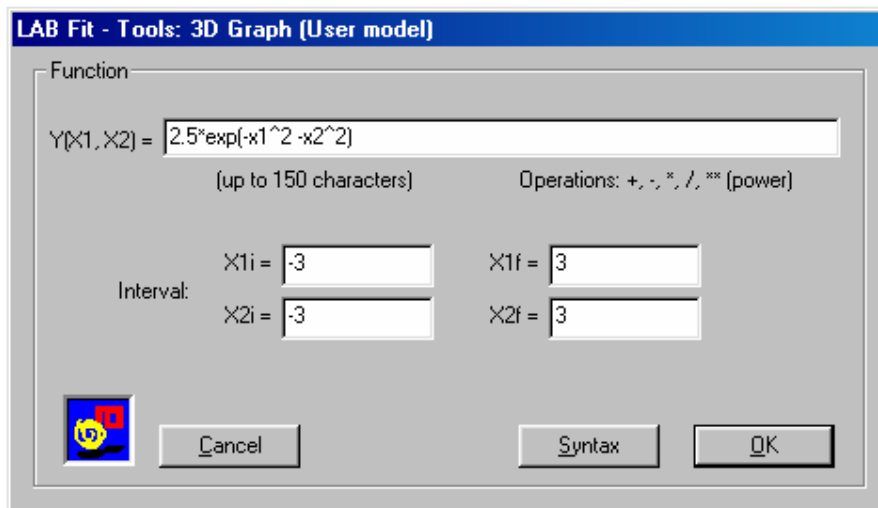
Then, at the “**Edit**” menu, it must be clicked on “**Copy**”, as it is shown at next.



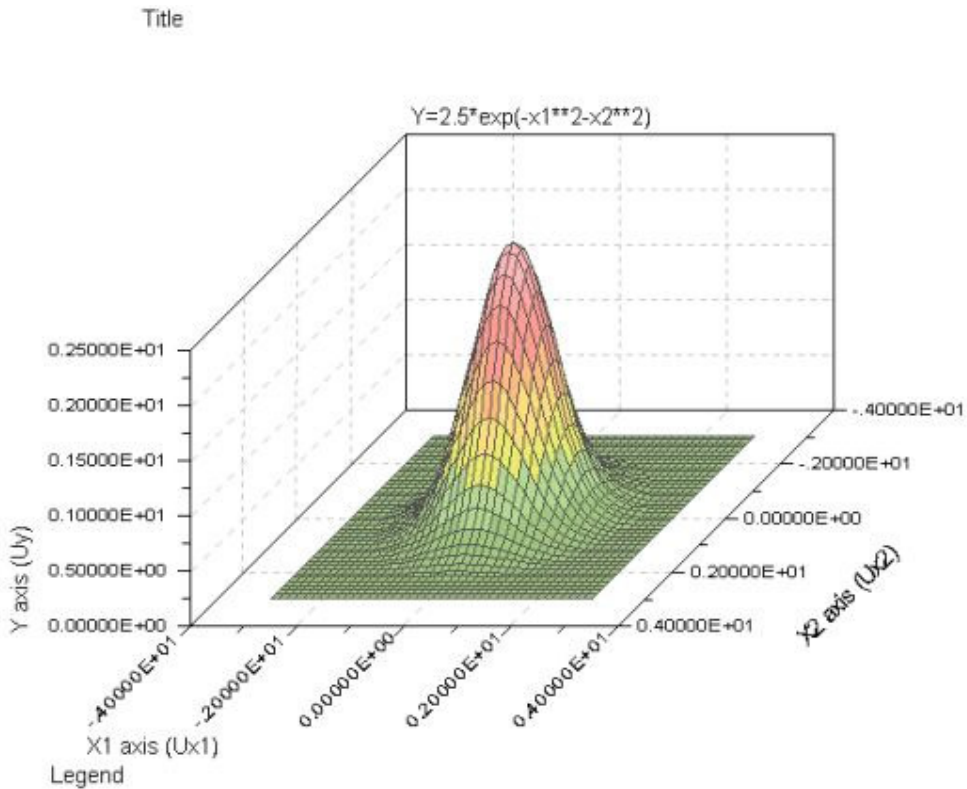
Then, it is just a matter of opening the document, and pasting the image that was stored at the clipboard.

3D Graph: User model (G 3D)

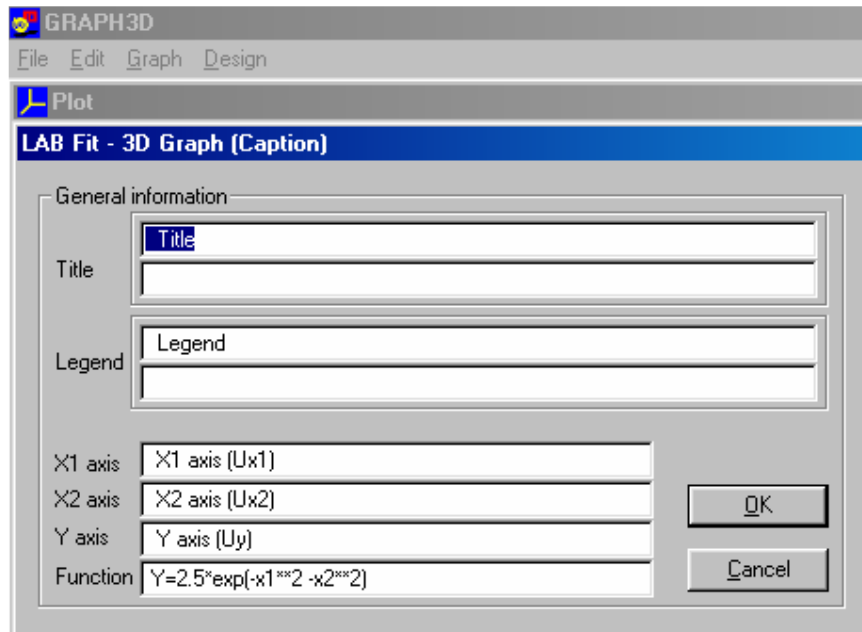
To plot a graph with 2 independent variables the user must, at the “**Tools**” menu, click on the “**3D Graph: User model**” option, or at the “**G 3D**” button. Then, the following message will appear: **‘Please: click on “graph” menu and set the parameters!’**. When “**OK**” is clicked, at the message box, and afterwards on the “**Graph**” item of the menu of the same name, the following dialog box will appear:



At the first edit box, the function of two variables (X1 and X2) , which the graph will be drawn must be written. At the following edit boxes, the interval limits of X1 and X2 must also be written. When “**OK**” is clicked the graph will be drawn.



At the same time that the 3D graph is being drawn, a new box for the final characterization appears (title, legend, axis and function definition):

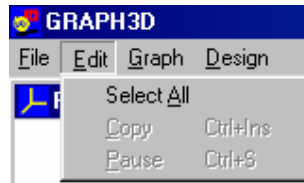


Once the 3D graph is characterized, there are two options to print it.

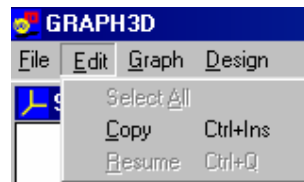
To use the **first option**, we must click on "Print window", at the "File" menu, but this option is only used to print only a **sketch**, because the printing is not of good quality: the printed picture will have the same resolution shown on screen.

The **second option** makes it possible to print a graph **with a better quality than the previous one**, what can be done by clicking on the “Superzoom in” item from the “Graph” menu. The graph will be, then, drawn again, but with a resolution much higher than the original one, occupying a much bigger space than the available screen size. After that, at the “File” menu, the user must click on “Print graph (superzoom)”.

To **paste** the graph on a document, the user must, at the “Edit” menu, select the “Select All” option as it is shown at the picture at next:



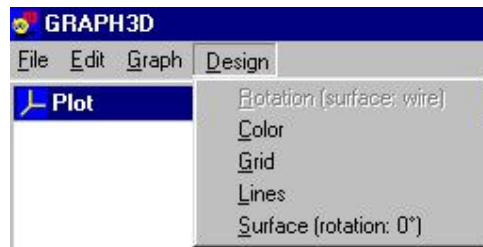
After, at the same “Edit” menu, we must click on “Copy”, as it is shown at next.



Then, it is only a matter of opening the document, and pasting the image that was stored at the clipboard.

The “Design” menu of the Graph3D

In case the user is plotting a 3D graph, some unique options can be chosen, that are shown at the “Design” menu, at next.



The “Rotation (surface: wire)” option makes it possible to rotate the graph in up to 45 degrees (the default is 0 degrees) but does not work for a solid mesh which is the default option. Whereas the “Color” option makes it possible to choose among six distinct colors (standard, blue, red, magenta, green and gray, the default is standard) for the drawing of the **wire frame** or the **solid mesh**. The “Grid” option makes it possible to draw grids at the X1-Y, X2-Y and X1-X2 planes (the default is with grids enabled) whereas, clicking on “Lines”, the user can indicate with how many lines the surface must be drawn (from 10 up to 100, the default is 40).